## Short Tutorial on Matlab

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## Part 5. Using S-function blocks in Simulink ${ }^{\circledR}$

I. Motivation: With the complexity of medium-size to large-size nonlinear models, it may be more efficient to use a set of differential equations written in an m-file. These m -files will be accessed by Simulink through the S -function block. Thus, this method mixes the advantages of an m -file which can be run directly by solvers such as ode45, with the graphical links to other Simulink blocks.

## II. Example System:

Suppose we want to model the nonisothermal CSTR,

$$
\begin{aligned}
& \frac{\mathrm{dC}_{\mathrm{a}}}{\mathrm{dt}}=\left(\frac{\mathrm{F}}{\mathrm{~V}}\right) \cdot\left(\mathrm{C}_{\mathrm{af}}-\mathrm{C}_{\mathrm{a}}\right)-\mathrm{k}_{0} \cdot \exp \left[-\frac{\mathrm{E}_{\mathrm{a}}}{\mathrm{R} \cdot(\mathrm{~T}+460)}\right] \cdot \mathrm{C}_{\mathrm{a}} \\
& \frac{\mathrm{dT}}{\mathrm{dt}}=\left(\frac{\mathrm{F}}{\mathrm{~V}}\right) \cdot\left(\mathrm{T}_{\mathrm{f}}-\mathrm{T}\right)-\frac{\Delta \mathrm{H}}{\rho \cdot \mathrm{C}_{\mathrm{p}}} \cdot\left[\mathrm{k}_{0} \cdot \exp \left[-\frac{\mathrm{E}_{\mathrm{a}}}{\mathrm{R} \cdot(\mathrm{~T}+460)}\right] \cdot \mathrm{C}_{\mathrm{a}}\right]-\left(\frac{\mathrm{U} \cdot \mathrm{~A}}{\rho \cdot \mathrm{C}_{\mathrm{p}} \cdot \mathrm{~V}}\right) \cdot\left(\mathrm{T}-\mathrm{T}_{\mathrm{j}}\right)
\end{aligned}
$$

We want to model this system in which we will treat the jacket temperature, $\mathrm{T}_{-} \mathrm{j}$, as the input (i.e. manipulated variable). We will also want to monitor concentration and temperature of the liquid in the CSTR as our outputs.

## III. Write the m-file.

Recall that we could model the process by writing an m-file to be used by Matlab solvers such as ode45. One such file, which we will name as reactor .m, is shown in Figure 1.

Test the model to make sure it works. For instance, with $T_{j}=55$ :

```
>> [t,x]=ode45(@reactor,[0 10], [0.1;40],[],55);
```

Note/Recall: The command-line specifies: a simulation-time span of [0 10], an initial-value column vector: [0.1;40], a null placeholder, [], for default options, and setting $T_{j}$ with a value equal to 55 .

```
function dx = reactor(t, x,Tj)
%
% model for reactor
%
    Ca = x(1) ; % lbmol/ft^3
    T = x(2) ; % OF
    Ea = 32400 ; % BTU/lbmol
    k0 = 15e12 ; % hr^-1
    dH = -45000 ; % BTU/lbmol
    U = 75 ; % BTU/hr-ft^2-oF
    rhocp = 53.25 ; % BTU/ft^3
    R = 1.987 ; % BTU/lbmol-oF
    V = 750 ; % ft^3
    F = 3000 ; % ft^3/hr
    Caf = 0.132 ; % lbmol/ft^3
    Tf = 60 ; % OF
    A = 1221 ; % ft^2
    ra = k0*exp(-Ea/(R* (T+460)))*Ca;
    dCa = (F/V)*(Caf-Ca)-ra;
    dT = (F/V)*(Tf-T)-(dH)/(rhocp)*ra...
        -(U*A)/(rhocp*V)* (T-Tj);
    dx =[dCa;dT];
```

Figure 1. File saved as reactor.m

## Remarks:

1. We treat $T_{j}$ as an argument/parameter. This is in anticipation that we will be varying $T_{j}$ later as an input/manipulated variable.
2. The arguments $\mathbf{x}$ and $d \mathbf{x}$ are column vectors for state and derivative, respectively.
3. Writing a model first for direct ODE45 implementation is advisable, specially for complex processes. This way, one can check the validity of the model, prior to its incorporation to a Simulink model.

## IV. Write an S-function file.

This file will also be saved as an m-file. It contains the protocol in which Simulink can access information from Matlab.

For our example, we show one such S-function file in Figure 2. We will save this file as reactor_sfen.m.

```
function [sys,x0,str,ts]=...
    reactor_sfcn(t,x,u,flag,Cinit,Tinit)
```

```
switch flag
    case 0 % initialize
        str=[] ;
        ts = [0 0] 0 ;
        s = simsizes ;
            s.NumContStates = 2 ;
            s.NumDiscStates = 0 ;
            s.NumOutputs = 2 ;
            s.NumInputs = 1 ;
            s.DirFeedthrough = 0 ;
            s.NumSampleTimes = 1 ;
    sys = simsizes(s) ;
    x0 = [Cinit, Tinit] ;
    case 1 % derivatives
    Tj = u ;
    sys = reactor (t,x,Tj) ;
    case 3% output
        sys = x;
    case {2 4 9}
    % 2:discrete
    % 4:calcTimeHit
                            % 9:termination
    sys =[];
    otherwise
    error(['unhandled flag =',num2str(flag)]) ;
end
```

Figure 2. File saved as reactor_sfen.m.
Let us deconstruct the S-function file given in Figure 2 to understand what the file needs to contain.

1. The first line specifies the input and output arguments.
```
function [sys,x0,str,ts]=...
    reactor_sfcn(t,x,u,flag, Cinit,Tinit)
```

As it is with any Matlab functions, the variable names themselves are not as crucial as the positions of the variables in the list.

## a) input arguments

(1) $t$ - the time variable
(2) $\mathbf{x}$ - the column-vector of state variables
(3) $\mathbf{u}$ - the column-vector of input variables (whose value will come from other Simulink blocks)
(4) $f l a g$ - indicator of which group of information and/or calculations is being requested by Simulink.

There are six types of request that Simulink performs, each of which is designated by an integer number:

| flag <br> value | Job/Data Request |
| :---: | :--- |
| $\mathbf{0}$ | Initialization: <br> a) <br> Setup of input/output vector sizes and <br> other setup modes <br> b) <br> Specification/calculation of initial <br> conditions for the state variables. |
| $\mathbf{1}$ | Derivative Equation Updating: <br> a) Calculations involving input vectors <br> b) Calculation of the derivatives |
| $\mathbf{2}$ | Discrete Equation Updating <br> (will not be used for our example) |
| $\mathbf{3}$ | Output Calculations: <br> Evaluating output variables as a function of <br> the elements of the state vector (and in <br> some case, also the elements of the input <br> vector) |
| $\mathbf{4}$ | Get Time of Next Variable Hit <br> (will not be used for our example) |
| $\mathbf{9}$ | Termination: <br> Additional routines/calculations at the end <br> of the simulation run. <br> (will not be used for our example) |

(5) Cinit, Tinit - additional supplied parameters.

In our case, these are the initial conditions for concentration and temperature.
Note: We do not specify what the values of the input arguments are. Their values will be specified by Simulink during a simulation run.

## b) output arguments

(1) sys - the main vector of results requested by Simulink. Depending on the flag sent by Simulink, this vector will hold different information.
$\left.\begin{array}{|l|l|}\hline \text { If } \mathbf{f l a g}=0 & \begin{array}{l}\mathbf{s y s}=[\mathbf{a}, \mathbf{b}, \mathbf{c}, \mathbf{d}, \mathbf{e}, \mathbf{f}, \mathbf{g}] \\ \text { where, } \\ \mathbf{a}=\text { number of continuous time states } \\ \mathbf{b}=\text { number of discrete time states } \\ \mathbf{c}=\text { number of outputs ( Note: this is not necessarily } \\ \text { the number of states) }\end{array} \\ \mathbf{d}=\text { number of inputs } \\ \mathbf{e}=0 \quad \text { (required to be 0, not currently used) } \\ \mathbf{f}=0 \text { (no) or 1(yes) for direct algebraic feed through } \\ \text { of input to output. ( this is relevant only if during } \\ \text { flag=3, the output variables depend algebraically } \\ \text { on the input variables.) } \\ =\text { number of sample times. ( for continuous } \\ \text { process, we set this equal to 1) }\end{array}\right]$

The next set of 3 output arguments are needed by Simulink only when $\boldsymbol{f l a g}=0$, otherwise they are ignored:
(2) $\mathbf{x} \mathbf{0}$ - column vector of initial conditions.
(3) str - need to be set to null. This is reserved for use in future versions of Simulink.
(4) ts - an array of two columns to specify sampling time and time offsets. Since our example will deal only with continuous systems, this will be set to [0 0] during initiation phase.
2. After the first line, the S -function file is split into the different cases determined by flag. As shown in Figure 3, we show the bare structure of the "containers" for the different cases. We have left out the details for case 1,2 and 3 . For case 2,4 , and 9 , we simply set sys=[]. The last two lines to catch an exceptional case where a bug occurs during the Simulink run.

```
switch flag
    case 0
        % . . .
    case 1 % derivatives
        % . . .
    case 3
        % . . .
    case {2 4 9}
        sys =[];
    otherwise
        error(['unhandled flag =',num2str(flag)]) ;
end
```

Figure 3.
Now, let us fill the details.
For case 0 (initialization),
a) define str, ts and $\mathbf{x 0}$

```
str=[] ;
ts = [0 0]
x0 = [Cinit, Tinit] ;
```

b) create a row vector which specifies the number of inputs and outputs, etc.

To aid in this, we invoke the simsizes command.
Without arguments, simsizes will creates a strucure variable which we can then fill with the required values:

| s.NumContStates | $=2$ | $;$ |
| :--- | :--- | :--- | :--- |
| s.NumDiscStates | $=0$ | $;$ |
| s.NumOutputs | $=2$ | $;$ |
| s.NumInputs | $=1$ | $;$ |
| s.DirFeedthrough $=0$ | $;$ |  |
| s.NumSampleTimes $=1$ | $;$ |  |

Using the command simsizes again with the structure variable as the argument actually translates the values in the structure, $\mathbf{s}$, into a row vector which gets sent to Simulink via sys:
$\square$
For case 1 (derivative calculations)

We set the input $\mathbf{u}$ to $\mathbf{T j}$ and then apply it to the m -file we wrote earlier, i.e.
reactor.m:

```
case 1
% derivatives
    Tj = u
sys = reactor(t,x,Tj)
```

For case 3 (output calculations)

```
case 3 % output
    sys = x;
```


## V. Insert the S-Function block into the Simulink.

In the Simulink Library browser, go to the [User-Define Functions] subdirectory. Then drag-drop the S-Function block (see Figure 4).

Double-click on the S-function block and fill in the parameters. Change the Sfunction name to reactor_sfen. Also, fill in the parameters. In our case, we input 0.1,40 (which is the value for Cinit and Tinit) as shown in Figure 5.


Figure 4.


Figure 5.

## VI. Add other Simulink blocks and simulate.



Figure 6.
Remark: In figure 6, we include a demux block (which stands for demultiplexer) to split the output vector to the 2 elements. In other applications where the input vectors has more than one element, we need a mux block (which stands for multiplexer). Both mux and demux blocks reside in the Signal Routing subdirectory of the Simulink Library browser.

